

# Public Economics

## Lecture 7: Taxation of capital

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- 3 Optimal capital income taxation
- 4 Taxation of inheritances

## 1 Introduction

Specific features of capital

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Wealth distribution

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## Specific features of capital

- Capital income is about  $\frac{1}{3}$  of national income (labor income is about  $\frac{2}{3}$ ) but distribution of capital income is much more unequal than labor income.  
Capital income inequality is due to differences in savings behavior but also inheritances received.  
Equity suggests it should be taxed more than labor.
- Capital Accumulation correlated strongly with growth (although causality link is not obvious) and capital accumulation might be sensitive to the net-of-tax return.  
Efficiency cost of capital taxation might be high.

- Capital more mobile internationally than labor.  
Most national income tax systems are residence based.  
Incidence falls on the owner who can only escape tax through tax evasion (tax heavens) or changing residence.  
Incidence is then partly shifted to labor if capital is mobile.
- Capital taxation is extremely complex and provides many tax avoidance opportunities.

# From flows to stock

- Saving is a flow and wealth is a stock.
- Three saving flows:
  - Personal saving:  
Individual income less individual consumption;
  - Corporate saving:  
Retained earnings = after tax profits – dividends;
  - Government saving:  
Taxes – expenditures.
- Taxes on savings might affect different savings flows differently:  
Savings subsidy through a tax credit can increase individual savings but decrease public saving.

# Wealth

- Capital income is the returns from wealth holdings.
- Wealth is made from:
  - Tangible assets:  
Residential real estate (land and buildings whose income is rents) and unincorporated business and farm assets (whose income is profits);
  - Financial assets: corporate stocks (whose income is dividends and retained earnings), fixed claim assets (corporate and govt bonds, bank accounts whose income is interests);
  - Liabilities: mortgage debt, loans, consumer credit, ...

# Wealth dynamic

$$W_t = W_{t-1} + r_{t-1}W_{t-1} + E_t + I_t - C_t,$$

where:

- $W_t$  is wealth at time (or age)  $t$ ;
- $C_t$  is consumption expenditure;
- $E_t$  is (net of taxes) labor income;
- $r_{t-1}$  is the average (net) rate of return of investments during previous period;
- $I_t$  is net inheritances (received gifts and bequests minus gifts given).

- $W_{t-1}$  can be written as:

$$W_{t-1} = W_{t-2} + r_{t-2}W_{t-2} + E_{t-1} + I_{t-1} - C_{t-1}.$$

- Thus,  $W_t$  can be rewritten as:

$$\begin{aligned} W_t = & E_t + I_t - C_t \\ & + (E_{t-1} + I_{t-1} - C_{t-1})(1 + r_{t-1}) \\ & + W_{t-2}(1 + r_{t-2})(1 + r_{t-1}). \end{aligned}$$

- Finally, assuming that  $W_0$  is null, we obtain:

$$W_t = \sum_{k=1}^t (E_k + I_k - C_k) \prod_{j=k}^{t-1} (1 + r_j)$$

$$W_t = \underbrace{\sum_{k=1}^t (E_k - C_k) \prod_{j=k}^{t-1} (1 + r_j)}_{\text{Life-cycle wealth}} + \underbrace{\sum_{k=1}^t (I_k) \prod_{j=k}^{t-1} (1 + r_j)}_{\text{Inheritance wealth}}$$

Differences in wealth and capital income due to:

- Age, past earnings, and past saving behavior:
- Net Inheritances received;
- Investment's rates of return.

# Wealth distribution

- Wealth inequality is very large.
- Financial wealth is more unequally distributed than (net) real estate wealth.
- Share of real estate wealth falls at the top of the wealth distribution.
- In the United States (situation is slightly better in France, but order of magnitude is similar), households' wealth is divided  $\frac{1}{3}$ ,  $\frac{1}{3}$ ,  $\frac{1}{3}$  for the top 1%, the next 9%, and the bottom 90%. Bottom  $\frac{1}{3}$  households hold almost no wealth.
- Wealth is more unequally distributed than income:  
Top 1% wealth income share in the United States is around 20%. Top 1% labor income share is around 15%.

# Taxes affecting wealth accumulation

- Taxes on flows:
  - Corporate income tax;
  - Individual income tax on capital income;
  - Taxes on capital transfers (e.g. housing transactions, giving to children).
- Taxes on stock:
  - Property tax.

Beside taxes, other factors affect wealth dispersion:

- Heterogeneity in tastes for saving: discount rate, time inconsistency, financial education;
- Rates of returns received on assets: traditional risk aversion, luck, but also financial education;
- Net inheritances and gift received.

## Life cycle wealth or inheritance wealth?

Which one is the most important to explain wealth inequality?

The question can be reformulated from two perspectives:

- Academic perspective:  
What accounts for wealth accumulation and inequality? Is widely used life-cycle model with no bequests a good approximation?
- Policy perspective:  
Should we tax capital income and/or inheritance? How should we design pension systems?

## Key elements of the debate on capital taxation

### Academic debate:

- Distributional concerns: capital income accrues disproportionately to higher income families;
- Efficiency concerns: capital tax distorts savings, business creation, capital mobility across countries.

### Public policy debate:

- Should we tax income rather than consumption?
- Should we encourage savings by cutting tax on capital income or with tax-favored savings vehicles?

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  - Basic mechanisms
  - Taxes and the dynamic of wealth
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## Basic mechanisms

- Any individual lives two periods and maximizes:

$$\mathbb{U} = u(c_1, l_1) + \delta u(c_2, l_2),$$

where  $c_t$  is consumption in period  $t$  and  $l_t$  is labor supply in period  $t$ .

- Saving technology allows to transfer wealth  $s$  from one period to the next:

$$\begin{aligned}s &= w_1 l_1 - c_1, \\ c_2 &= w_2 l_2 + (1+r)s,\end{aligned}$$

where  $w_t$  is wage rate in period  $t$  and  $r$  is the interest rate.

- The intertemporal budget constraint can be written as:

$$c_1 + c_2 \frac{1}{1+r} \leq w_1 l_1 + w_2 l_2 \frac{1}{1+r}.$$

- With a tax  $\tau_c$  on consumption, the budget constraint becomes:

$$(1 + \tau_c) \left[ c_1 + c_2 \frac{1}{1+r} \right] \leq w_1 l_1 + w_2 l_2 \frac{1}{1+r}.$$

- With a tax  $\tau_l$  on labor income, the budget constraint becomes:

$$c_1 + c_2 \frac{1}{1+r} \leq \left[ w_1 l_1 + w_2 l_2 \frac{1}{1+r} \right] (1 - \tau_l).$$

- Consumption and labor income taxes are equivalent if

$$1 + \tau_c = \frac{1}{1 - \tau_l}.$$

- Both taxes distort only the labor-leisure choice.

- With a tax  $\tau_k$  on capital income, the budget constraints becomes:

$$c_1 + c_2 \frac{1}{1 + r(1 - \tau_k)} \leq w_1 l_1 + w_2 l_2 \frac{1}{1 + r(1 - \tau_k)}.$$

- The capital income tax distorts only the intertemporal consumption choice.
- With a comprehensive tax  $\tau$  on income, the budget constraint becomes:

$$c_1 + c_2 \frac{1}{1 + r(1 - \tau)} \leq \left[ w_1 l_1 + w_2 l_2 \frac{1}{1 + r(1 - \tau)} \right] (1 - \tau).$$

- The comprehensive tax distorts both the labor-leisure and the intertemporal consumption choices.
- The comprehensive tax imposes a “double” tax on earnings and savings.

# Taxes and the dynamic of wealth

- What is the effect of taxation on capital accumulation?
- Transit through savings.

## Capital income taxation

- Same reasoning as for a change in the interest rate.
- Assume that labor supply is fixed and  $r$  goes up:
  - Substitution effect:  
The relative price of  $c_2$  decreases, so  $c_2$  goes up and  $c_1$  goes down: savings increase.
  - Wealth effect:  
The total price of consumption decreases, so  $c_1$  and  $c_2$  go up: savings decrease.
  - Human wealth effect:  
The present discounted value of labor income decreases, both  $c_1$  and  $c_2$  decrease: saving increase.
- Total net effect is theoretically ambiguous.
- Capital income taxation has ambiguous effects on savings.

## Labor and consumption taxes

- Labor and consumption choices are equivalent under  $\tau_c$  and  $\tau_l$  if

$$1 + \tau_c = \frac{1}{1 - \tau_l},$$

but savings pattern is different.

- For simplicity, assume  $w_2 = 0$  and  $l_1 = 1$ .
- Under consumption tax, the (binding) budget constraint is:

$$(1 + \tau_c) \left[ c_1 + c_2 \frac{1}{1 + r} \right] = w_1.$$

And consumption is:

$$c_1^c = \frac{w_1 - s_c}{1 + \tau_c} \quad \text{and} \quad c_2^c = s_c \frac{1 + r}{1 + \tau_c}.$$

- Under labor income tax, the budget constraint is:

$$c_1 + \frac{c_2}{1+r} = (1 + \tau_l)w_1.$$

And consumption is:

$$c_1' = w_1(1 - \tau_l) - s_l \text{ and } c_2' = (1 + r)s_l.$$

- Since consumption at times 1 and 2 is equal across cases:

$$s_l = \frac{s_c}{1 + \tau_c}.$$

- Savings are higher with the consumption tax than with the labor income tax. This arises because of taxation timing.

## Transition from labor to consumption tax

- Overlapping generations model of a closed economy with two generations (old and young) at each period.
- Capital stock is due to life-cycle savings  $s$ .
- Start a labor tax  $\tau_l$  and switch to a consumption tax  $\tau_c$ .
- The old generation (at time of transition) would have paid nothing during the current period in labor tax regime but now has to pay tax on  $c_2$ .
- For the young [and future generations], the two regimes look equivalent so they now save more and increase the capital stock.
- However, this increase in capital stock comes at the price of hurting the old who are taxed twice

- Suppose the government wants to keep the old as well off as in previous system by exempting them from consumption tax during their old days.
- This creates a deficit in government budget equal to:

$$d = \tau_l w_1 - \tau_c c_1 = \tau_c w_1 / (1 + \tau_c) - \tau_c c_1 = \tau_c s_l.$$

- Extra saving by the young is  $s_c - s_l = \tau_c s_l$  and exactly equals government deficit.
- Full neutrality result: extra savings of young is equal to old capital stock plus new government deficit; that is, there is no change in the aggregate capital stock during the transition.

## Saving and taxation in a life-cycle model

Auerbach, Alan J & Kotlikoff, Laurence J, 1987. "Evaluating Fiscal Policy with a Dynamic Simulation Model," American Economic Review, American Economic Association, vol. 77(2), pages 49-55, May.

- Intertemporal computational general equilibrium model.
- Life cycle without bequest.
- Only one individual per cohort, representative agent model: useful for redistribution analysis across cohorts but not within cohorts.
- Stock of wealth equals life cycle savings.
- Labor income tax distorts labor supply, capital income tax distorts savings choice.
- Tax reform simulations: move (without transitional compensation) from a comprehensive income tax to either (i) a pure consumption tax, (ii) a pure wage income tax, (iii) pure capital income tax.

- Results:
  - Consumption tax is best because no compensation of the old generations.
  - Wage income tax has limited impact on capital stock.
  - Capital income tax is worst because it hurts current generation (double tax), benefits next generation (implicit levy of previously accumulated capital), but hurts future generations (inefficient).
- Key lessons: Compensation rules during the transition and whether tax changes are anticipated or not have large impact on conclusions.

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  - Ramsey tax in a life cycle model
  - Endogenous capital stock
  - Additional insights
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# Optimal capital income taxation

Complex problem with many different academic approaches:

- Life-cycle models with linear and non-linear tax;
- Models with bequests (including the infinite horizon model);
- Models with future earnings uncertainty.

Bigger gap between theory and policy practice than in the case of static labor income taxation.

## Ramsey tax in a life cycle model

Mervyn A. King, 1980. "Savings and Taxation," NBER Working Papers 0428, National Bureau of Economic Research, Inc.

- Ramsey model with a representative agent and linear taxes on labor and savings to raise an exogenous amount of revenue.
- The representative agent chooses  $c_1$ ,  $c_2$ , and  $l$  in order to maximize:

$$u(c_1, c_2, l),$$

$$\text{s.t. } c_1 + \frac{c_2}{1+r(1-\tau_k)} = wl(1 - \tau_l).$$

- This leads to the indirect utility function:

$$V(q, w(1 - \tau_l)),$$

where  $q = \frac{1}{1+r(1-\tau_k)}$  is the post-tax price of  $c_2$ .

- Optimal tax rates can be obtained by solving the standard Ramsey problem, i.e. choose  $\tau_l$  and  $\tau_k$  in order to maximize:

$$\begin{aligned} & V(q, w(1 - \tau_l)), \\ \text{s.t. } & w/\tau_l + (q - p)c_2 \geq g, \end{aligned}$$

where  $g$  is exogenous tax revenue requirement and  $p = \frac{1}{1+r}$  is the pre-tax price of  $c_2$ .

- Combining the two first order conditions and getting rid of the Lagrange multiplier, we get:

$$\frac{r\tau_k}{1+r}(\sigma_{l2} - \sigma_{22}) = \frac{\tau_l}{1-\tau_l}(\sigma_{ll} - \sigma_{2l}),$$

where:

$$\sigma_{ll} = (w(1-\tau_l)/l)\partial l/\partial(w(1-\tau_l)) > 0$$

is the compensated elasticity of labor supply with respect to the net wage rate, and:

$$\sigma_{22} = (q/c_2)\partial c_2/\partial q < 0,$$

$$\sigma_{l2} = (q/l)\partial l/\partial q,$$

$$\sigma_{2l} = (w(1-\tau_l)/c_2)\partial c_2/\partial(w(1-\tau_l)).$$

- Formula defines relative optimal rates of taxation on labor and capital (absolute levels depend on  $g$ ).

- As we know little about cross elasticities, let us assume that they are zero.
- The optimal formula simplifies to:

$$-\frac{r\tau_k}{1+r}\sigma_{22} = \frac{\tau_l}{1-\tau_l}\sigma_{ll}.$$

- Inverse elasticity rule:  
If  $\sigma_{ll} \ll |\sigma_{22}|$ , then  $\tau_k$  should be small relative to  $\tau_l$ .
- What matters is the relative size of elasticities.

## Endogenous capital stock

- The optimal dynamic capital stock  $k$  is given by the modified Golden rule:

$$r = f'(k) = \delta,$$

where  $\delta$  is the discount rate.

- Optimal  $k$  can be attained in steady state using public debt policy.
- In that case, optimal  $\tau_k$  and  $\tau_l$  are given by previous rule.

- If the government cannot use debt policy, then optimal dynamic capital level may not be attained because savings equal capital  $s_t = k_t$ .
- In that case, tax formulas need to be modified and optimal tax rates reflect:
  - The trade-off between conventional (intra-generational) efficiency losses;
  - The failure to achieve the dynamic optimality condition on capital stock (inter-generational efficiency trade-off).
- Effect on capital tax rate level is actually ambiguous.

## Remarks on the previous model

- No redistributive concerns:  
The model can be extended to the multi-person case.  $\tau_k$  will be higher if capital (and capital income) is concentrated among the rich.
- No bequests:  
This model does not capture an important aspect of wealth accumulation and justification for redistribution.
- Only a two period model:  
If more periods are introduced, then optimal tax formula would be more complex.
- No heterogeneity in the population:  
If individuals differ in ability (wage rate) and discount rate, then it may be optimal to introduce a small savings tax on high earners or a small savings subsidy on low earners.

## Limits of the life cycle framework

- It may seem fair to not discriminate against savers if labor earnings is the only source of inequality and is already taxed non-linearly.
- In reality, capital income inequality is also due to:
  - Difference in rates of returns;
  - Shifting of labor income into capital income;
  - Inheritances.

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  - Behavioral responses
  - Accidental bequests
  - Warm glow bequests
  - Manipulative bequests
  - Dynastic models

- Definitions: donor is the person giving, donee is the person receiving.
- Inheritances and inter-vivos transfers raise difficult issues:
  - Inequality in inheritances contributes to economic inequality:  
Seems fair to redistribute from those who received inheritances to those who did not;
  - However, it seems unfair to double tax the donors who worked hard to pass on wealth to children
- Double welfare effect: inheritance tax hurts donor (if donor is altruistic to donee) and donee (which receives less).

## Behavioral responses

Potential behavioral response effects of inheritance tax:

- Reduces wealth accumulation of altruistic donors (and hence tax base). No very good empirical evidence.
- Reduces labor supply of altruistic donors (less motivated to work if cannot pass wealth to kids). No very good empirical evidence.
- Induces donees to work more through income effects. Some empirical evidence.

Its important to understand why there are inheritances to decide on optimal inheritance tax policy. There are four main models of bequests: (i)accidental, (ii) warm glow, (iii) manipulative bequest motive, (iv) dynastic.

## Accidental bequests

- People die with a stock of wealth they intended to spend on themselves. Such bequests arise because of imperfect annuity markets.
- Annuity is an insurance contract converting lump-sum amount into a stream of payments till end of life (insurance against risk of living too long).
- Annuity markets are imperfect because of adverse selection or behavioral reasons (inertia, lack of planning).
- Public retirement programs are in general annuities.
- Bequest taxation has no distortionary effect on behavior of donor and can only increase labor supply of donees (through income effects).
- Strong case for taxing bequests heavily.

## Warm glow or altruistic bequests

- Let us consider the following utility function:

$$u(c) - h(l) + \delta v(b),$$

where  $c$  is life-time consumption,  $l$  is labor supply,  $b$  is net-of-tax bequests left to next generation, and  $v(b)$  is warm glow utility of bequests.

- Neglecting taxes on labor income, the budget constraint can be written as:

$$c + \frac{b}{(1+r)(1-\tau)} \leq wl,$$

where  $r$  is the interest rate and  $\tau$  the tax on bequest.

- Suppose first that  $b$  is not really bequeathed but used for “after-life” consumption (e.g., funerary monument of no value to next generation).
- Then  $b$  should not be taxed:  $\tau = 0$ .
- Suppose now that  $b$  is given to a heir who derives utility  $v^{\text{heir}}(b)$ .
- This means that  $b$  creates a positive externality and should be subsidized:  $\tau < 0$ .
- But, if past inheritances come from untaxed labor income, then it is desirable to tax inheritances.

## Manipulative bequests

- Parents use potential bequest to extract favors from children.

Bernheim, B Douglas & Shleifer, Andrei & Summers, Lawrence H, 1985. "The Strategic Bequest Motive," *Journal of Political Economy*, University of Chicago Press, vol. 93(6), pages 1045-76, December.

- Show that number of visits of children to parents is correlated with bequeathable wealth but not annuitized wealth of parents.
- Bequest becomes one additional form of labor income for donee and one consumption good for donor.
- Inheritances should be taxed as labor income for donees.

## Dynastic or infinite horizon models

- Basic idea: today's individual utility is the sum of the living agent's utility, the agent's utility, and discounted next generations' utilities.

Chamley, Christophe, 1986. "Optimal Taxation of Capital Income in General Equilibrium with Infinite Lives," *Econometrica*, Econometric Society, vol. 54(3), pages 607-22, May.

Judd, Kenneth L., 1985. "Redistributive taxation in a simple perfect foresight model" *Journal of Public Economics*, Elsevier, vol. 28(1), pages 59-83, October.

- Show that optimal tax on capital should converge to zero as a positive value would lead to zero capital for distant generations.
- But such models are not really useful to think about optimal capital taxation.

## Further readings

- On inheritances:  
Thomas Piketty, 2011. "On the Long-Run Evolution of Inheritance: France 1820–2050," *The Quarterly Journal of Economics*, Oxford University Press, vol. 126(3), pages 1071-1131.
- On tax heavens:  
Gabriel Zucman, 2012. "The missing wealth of nations: Are Europe and the U.S. net debtors or net creditors?," PSE Working Papers halshs-00565224, HAL.
- On income inequality:  
Thomas Piketty, 2003. "Income Inequality in France, 1901-1998," *Journal of Political Economy*, University of Chicago Press, vol. 111(5), pages 1004-1042, October.  
Thomas Piketty & Emmanuel Saez, 2003. "Income Inequality In The United States, 1913-1998," *The Quarterly Journal of Economics*, MIT Press, vol. 118(1), pages 1-39, February.

End of lecture.

Lectures of this course are inspired from those taught by R. Chetty, G. Fields, N. Gravel, H. Hoynes, and E. Saez.